The Grammar of Measurement

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1. Partitives and Compounds

The phrase 2 liters of oil is a pseudopartitive. It includes a measure phrase, 2 liters, and a substantive indicating what kind of substance is measured. I can use 2 liters of oil to talk about oil whose volume is 2 liters. Suppose I wanted instead to talk about oil whose temperature was 90 degrees. I should be able to say *90 degrees of oil, but I can’t. Instead, I have to say 90-degree oil. The absence of of indicates that this is not a pseudopartitive. The absence of number marking on degree suggests that it is a nominal compound. What is it about 90 degrees that prevents its use in pseudopartitives but allows it compounds?

too much gold is also a pseudopartitive, which, for reasons not relevant here, needs no of. Parsons(1970) observed that expressions like these are ambiguous about how the gold is being measured. It could be too much gold by weight or too much by volume. But if it can mean gold which is too heavy or gold whose volume is excessive, why can’t it mean gold which is too dark? “You put too much gold in the ring,” I would say to the jeweler, to mean that the gold in the ring is darker than I wanted. But I can’t use too much gold in that way, and it isn’t because much is unable to quantify over degrees of darkness, for that is just what it seems to do when I say “the gold is much darker than I had expected.”

Inches and feet are appropriate units for measurements taken in various dimensions. Nevertheless, while I can use a foot of cable to speak of length, if I’m concerned with the diameter of the cable, why must I say quarter inch cable, again employing a compound, which is of-less and devoid of number marking, and where the indefinite article is omitted before quarter? And if 2 feet of cable

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concerns the length of the cable, how is it that 2 feet of snow tells us about the depth of the snow and nothing about the length?

Terminological Note. ‘pseudopartitive’ and ‘compound’ are descriptive syntactic labels, while ‘measure phrase’ and ‘substantive’ are semantic labels. I use ‘measure phrase’ to include not only noun phrases whose head is a term of measure such as gallon or ounce, but also adjectival phrases such as much, too much and so many as well as expressions such as a lot or a little or a truckload. ‘substantive’ is used to cover noun phrases like those following of in a pseudopartitive as well as the head nouns of compounds. Although both compounds and pseudopartitives do not have to be formed with measure phrases, until further notice, I restrict consideration to those that are. In section 5, we will attempt a more detailed analysis of the syntax of partitives and compounds.

2. Monotonic systems of measurement

A system of measurement is one in which elements of an ordered set of measurements, a scale, are assigned to a domain of entities, based on some property. The goal is for the ordering of the measurements to reflect the degree to which entities in the domain have the property in question. Higher length measurements are assigned to longer objects, higher temperatures to hotter ones and so on. Now while all measurement systems mirror the degree to which an entity has the property in question, some but not all mirror as well the intuitive part structure of the stuff being measured. For example, if a quantity of oil has a certain volume, then every proper subpart of it will have a lower volume and superparts will have larger volumes. On the other hand, if the oil has a certain temperature, there is no reason to expect that proper parts of it will have lower temperatures. We will call a property monotonic if it tracks part-whole relations. Volume is monotonic and temperature is non-monotonic. Pseudopartitives may be based on monotonic properties such as volume of oil, hence 2 liters of oil is good but never on non-monotonic properties, hence *90 degrees of oil is bad. Exactly the reverse is the case for compounds in English, for while the non-monotonic 90 degree oil is felicitous, compounds cannot be formed when the interpretation is based on a monotonic property: *2 liter oil.

A monotonic property was just defined as one that tracks the part-whole structure of its domain, but which part-whole structure? To see the bite of this question consider a spool of computer cable. If we take its parts to be linear segments, then length is monotonic, but diameter is not, and we correctly predict that 2 feet of cable being a pseudopartitive would have to be interpreted in terms of length, not diameter, while ¼ inch cable, being a compound, would have to be interpreted in terms of diameter and not length. Things work out nicely if we suppose a part structure given in terms of linear segments. Assume instead that our parts include slices running the length of the spool or worse, any portion of cable. Now the monotonicity facts change and we fail to explain our second set of puzzles.

The upshot of the previous paragraph is that pseudopartitives and compounds and, as we shall see, their cross-linguistic kin, all presuppose a
particular part-whole structure for the stuff being measured. In the case of the pseudopartitive, the property which forms the basis for measurement has to be monotonic relative to the given part-whole structure, for compounds it needs to be non-monotonic. The choice of the part-whole structure will often be given by convention, as in the cable example. But we should also expect it to be sensitive to facts salient in the discourse. Witnessing a growing pool of oil seeping out of the ground, we may report its progress by declaring there to be 10 inches of oil, by which we intend to report that the pool has a radius of 10 inches. The relevant parts are concentric subpools and so in this case radius is monotonic, for if A is a subpool of B, then A’s radius is less than B’s. This is a very specialized context. The limiting case, where context and convention make no contentful contribution, is where you have a complete mereology. That’s what we had when we initially spoke of oil and gold.

In 2 inches of snow, depth provides the basis for measurement. Given that 2 inches of snow is a pseudopartitive, we can reason backwards that the relevant part-whole structure is one that makes depth monotonic, one in which the proper parts are layers of snows. Since presumably this has to do with how we think about fallen snow, we should find the same situation with other snowy pseudopartitives. That is why when I say too much snow fell, I convey that the depth was excessive. Similarly, if two inches of snow fell on Florida and 10 inches of snow fell on Rhode Island, I can say that Rhode Island got more snow than Florida, even though the surface area and the mass of Florida snow exceeds that of Rhode Island. I’ve assumed, not without precedent (e.g. Jackendoff 1977), that too much snow and more snow than Florida got are pseudopartitives, despite the lack of of. Our gold puzzles support this hypothesis. Recall that too much gold allows for mass and volume interpretation, which are monotonic systems for gold, but not darkness. Darkness is non-monotonic since there is no guarantee that any subpart of a lump of gold will be less dark than the lump itself. Darkness is non-monotonic, so a pseudopartitive like too much gold cannot be based on that kind of measurement.

Krifka(1989)² points out the contrast between five ounces of gold and *twenty carats of gold. The difference, he claimed, was due to the fact that ounce but not carat denotes an extensive measure function. He credits Cartwright(1975) with the introduction of measure functions in the semantics of measure phrases. We’ll have a bit more to say about this below. One of the requirements for extensivity is that the measure function be additive. If the band weighs 1 ounce and the diamond weighs ¼ of an ounce, then the ring weighs 1¼ ounces. This doesn’t work with carat ratings (n carat gold is n 24ths pure gold). Lønning(1987) was concerned with “how much of mathematics should be part of the semantics” and so he considered various alternatives to additivity, including what he called ‘monotonicity’. A function that gives ounce measurements is monotonic in this sense because if a is part of b and a weighs n ounces and b weighs m ounces, then n is less than m. I got the idea of monotonicity from Lønning, but I was concerned with how much of measurement practice should be part of this story, given that it would apply to adjectival measure phrases as well.

² I am grateful to Peter Lasersohn for urging me to take a look at Krifka(1989).
For me, monotonicity is not a characteristic of the measurement system, but rather a characteristic of the property on which the system is based. Early discussions of measurement looked at monotonic properties as a basis for measurement and later this became a constraint on measurement schemes (Díez 1997).

3. The Mass-Count Distinction

The expressions considered so far all contain a measure phrase such as 2 feet or too much as well as a substantive. So far, we’ve taken the job of the substantive to name the kind of stuff that is measured. I’d like to suggest now that the choice of a particular part-whole relation is also settled in the course of interpreting the substantive. This may seem at first unnatural, for surely the restriction to layers of snow or linear segments of cable has to do with how we conceive of fallen snow and our practices concerning cable and not anything to do with the English words snow and cable. But the motivation for this move comes not from these examples, but from an examination of the differential behavior of mass and count nouns in pseudopartitives and compounds. While we can say 2 hours of work and 2 pages of prose, if we replace the mass nouns with related count nouns we arrive at the impossible pseudopartitives *2 hours of job and *2 pages of story. These contrast with the corresponding compounds which are good: a 2 hour job, a 2 page story. Likewise, it is rude to announce the birth of 7 pounds of baby but a 7-pound baby is perfectly welcome.

Since the difference between a count and a mass noun is commonly taken to be a reflection of the salient part-whole relation, it seems worthwhile to try to account for these facts in terms of monotonicity. The leading idea would be that the extensions of singular count nouns are atomic, they fail to offer anything but a trivial part-whole relation. Monotonicity fails in these cases because it requires a part-whole relation to work off of. Pseudopartitives require monotonicity, so they fail with count nouns, while compounds abhor monotonicity and so they succeed with count nouns.

The restrictions discussed in the previous section can now be elaborated as follows. A pseudopartitive may be interpreted in terms of a measurement system if the denotation of the substantive comes with a part whole relation and the basis for the measurement is monotonic within the universe of the substantive with respect to its part-whole relation. Compounds require that these conditions not obtain, either because the substantive doesn’t come with a part whole relation or because it does come with one but the measurement system is not monotonic within the universe of the substantive with respect to the part-whole relation. This statement presupposes that noun extensions are potentially structured objects, with a universe of elements and a part-whole relation. For singular count nouns there is no part-whole relation, but for mass nouns there is. Furthermore, the universe and the part whole relation are partially pragmatically determined. In other words, when discussing fallen snow, the extension of snow just is a set of more or less continuous layers of snow. On the standard account, by contrast, the extension of snow includes all the bits of snow and the part-whole relation is just
material-part. Let’s assume then that context can narrow down the standard extension in such a way that no material is lost (the sum of all elements in the universe of the restricted structure is the same as in the unrestricted structure) and no new individual part-whole relations are added (if a is part of b in the restricted structure, a is part of b in the unrestricted one).

Given that singular count nouns never provide a non-trivial part-whole relation, they will always be bad in pseudopartitives and they will always be good in compounds. In fact, they will be good in compounds even when a corresponding mass noun is not. This leads to the following contrasts:

<table>
<thead>
<tr>
<th>(1)</th>
<th>*2 hour work</th>
<th>2 hour job</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>*2 liter oil</td>
<td>2 liter tank</td>
</tr>
<tr>
<td></td>
<td>*2 lb flour</td>
<td>2 lb rock</td>
</tr>
<tr>
<td></td>
<td>*2 page poetry</td>
<td>2 page poem</td>
</tr>
</tbody>
</table>

In each of these cases, the mass version is impossible because the basis for the measurement (duration, volume, weight, or page count) is monotonic on the part-whole relation. The count versions are possible, because the part-structure makes these same properties non-monotonic on the atomic part-structure associated with count nouns. In a sense, it’s the measure phrase that explains why 20° salt water is possible while it’s the noun that explains why 2 lb rock is.

Again following standard practice, we take plural nouns as coming with a part-whole structure given by the plural-part relation (the relation I bear to the plurality consisting of you and me). This means that they should behave more like mass nouns than like their singular counterparts. This is borne out in the case of pseudopartitives. 2 kilos of marbles contrasts with *10 degrees of ice cubes. But how do we explain the grammaticality of 7-pound babies given that *7-pound flour is out? The answer is that in 7-pound babies the plural marker has scope over the entire compound, in effect we have pluralized 7-pound baby. The interpretation is indeed one in which each baby weighs 7 pounds.

A predicative definite noun phrase never is true of more than one entity. In that case, the part-whole structure of its extension would have to be atomic, like that of a singular count noun and so we should not expect to find a definite noun phrase functioning as a substantive in a pseudopartitive. How then can we explain things like 4 pounds of the oranges or 2 pages of the first story? These are examples of true partitives which at least since Selkirk(1977) have been distinguished syntactically from pseudopartitives. Below we will take up some of the syntactic details, for now it should suffice to use the behavior of of to argue for the distinction. While pseudopartitive of does not occur with adjectival measure phrases (too much gold), true partitive of is not so fickle (too much of the gold). In recipe English, the difference is seen with nominal measure phrases as well. There we find 2 lbs butter but not *2 lbs the butter. And if one ventures outside of English (and Romance) one finds the difference with nominal measure phrases more robustly. Dutch, for example, distinguishes een kilo appels ‘a kilo of apples’ from een kilo van deze appels ‘a kilo of these apples’.
According to Ladusaw(1982), the true partitive of is meaningful. It combines with a definite noun phrase to form a predicate true of the parts of the referent of the noun phrase. Rephrasing slightly, the meaning of partitive of applies to the meaning of a definite noun phrase to deliver a universe consisting of the parts of the referent and the part-whole relation. Taking this unit to be our substantive, we now find contrasts like the ones we saw with the pseudopartitive: 2 ounces of the salt water versus *2° of the saltwater; 2 minutes of the strenuous exercises versus *4 o’clock of the exercises. On this way of thinking, our monotonicity constraints apply to all partitives, true and pseudo alike. The substantive in a pseudopartitive is just a noun phrase, and it’s extension must include a part-whole relation relative to which the basis for measurement is monotonic. The substantive in a true partitive consists of true-partitive-of combined with a definite noun phrase. The extension of this combination includes a part-whole relation relative to which the basis for measurement is monotonic.

Let’s take stock. Measure phrases combine with nouns in two different ways in English. In either case, the interpretation relies on some property that elements in the extension of the noun possess to varying degrees and in virtue of which a measurement can be made, a measurement whose result is described by the measure phrase. This property, the basis for measurement, must obey opposing restrictions in the two constructions. In one case, partitives, it must be monotonic relative to the part-whole structure given by the meaning of the noun it combines with, in the other case it must not be monotonic. This has a number of consequences including the following. Measure phrases from the realm of temperature combine with nouns in the compound-mode, but not in the partitive-mode. Measure phrases from the realm of volume combine with mass nouns in the partitive-mode, but not in the compound-mode. Singular count nouns offer no part-whole relation, hence they are always allowed in a compound and absent the intervention of a true partitive of they are always excluded from the partitive. Finally, if plurals are used, the measure phrase will apply distributively in the compound (6 ounce pebbles), but collectively in the partitive (6 ounces of pebbles).

Ultimately, it would be nice to know where these monotonicity restrictions come from and how they relate to the syntax of these constructions. In the following two sections, we will elaborate on the interpretation of measure phrases and the syntax of partitives. Following that we will offer some ideas about the place of monotonicity in the grammar.

4. Measure Phrases

As Jackendoff(1977) pointed out, measure phrases have a wide distribution. Degree phrases and prepositional phrases are just two contexts outside the ones we’ve considered so far in which measure phrases appear:

3 Actually, as Barker(1998) notes, what is required is a noun phrase that denotes a proper principal ultrafilter. This includes definites as well as singleton indefinites.
(2) $2$ more expensive, 2 lbs too heavy that much faster, much too spicy

2 feet away, 2° below, $2$ over that much above the house

This pattern of distribution is by no means peculiar to English. It occurs in such diverse languages as Bangla (Bhattacharya 1999), Hebrew, Hindi, Japanese and Polish. A possible explanation for why measure phrases are cross-categorial is that they have a uniform semantics and that the meaning in question happens to be called for in various contexts. This is a fairly pedestrian idea nevertheless it is one that I think has not yet been pursued and which seems worthy of consideration. I will attempt this beginning with a semantics of measure phrases worked out for the comparative. A reason to choose the comparative as the starting point is that of the various contexts where measure phrases are possible, the comparative is the least restricted. Note, for example, that while the availability of a measure phrase in the partitive is constrained by monotonicity, the comparative has no such restriction. I do not yet know whether the comparative is in fact the least marked context for measure phrases, from an historical and a typological perspective.

In Schwarzschild and Wilkinson(2002), we analyzed measure phrases in comparatives as predicates of parts of scales. To fix on an image, think of uses of expressions like 2 inches to talk about intervals of a ruler:

```
1 2 3 4 5 6 7 8 9 10 11 12

←2 in. → ←2 in. →
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The idea is to draw an analogy with adverbs of duration. The following examples illustrate the analogy.

(3) He shot the sheriff [2 hours] before he shot the deputy.
(4) Rod A is [2 inches] longer than rod B is.

In (3), 2 hours is predicated of the interval on the time line between the two shootings. In (4), 2 inches is predicated of the interval on the scale between where B is and where A is. This view extends to adjectival measure phrases as well. In (5) below:

```
1 2 3 4 5 6 7 8 9 10 11 12

←2 in. → ←2 in. →
```

In that paper we argue for an analysis of comparatives based on intervals rather than points on a scale, in analogy with the move from moments to intervals in tense semantics. The theory there was chiefly motivated by examples in which quantifiers appear in comparative than clauses as in Irving was closer to me than he was to most of the others. The crucial intuition is that there may not be some particular distance such that most of the others are that distance away from me, but there is a range such that the distance from me to most of the others lies in that range.
Rod A is [much] longer than rod B is.

*much* tells us that the size of the interval on the scale between where B is and where A is is large. On this view, *much* has a semantics quite like that of *long*. Both adjectives apply to extended entities, with *much* restricted to abstract, scale parts. Since both are gradable, we find *too long, so long, that long* alongside of *too much, so much, that much*. And in both cases, when no degree word such as *too or that* is present, one gets a ‘higher than expected’ reading. So *if the diamond were that much heavier* contrasts with *if the diamond were much heavier* in the same way as *if the necklace were that long* contrasts with *if the necklace were long*.

This view of measure phrases is based on the semantics for comparatives. Zwarts(1997) independently came to a very similar conclusion about measure phrases in his analysis of the semantics of prepositions. My hypothesis that measure phrases have a uniform semantics amounts now to the claim that, regardless of its external or internal syntax,

(6) a measure phrase just is a predicate of scalar intervals.

Jackendoff(1977) and Klooster(1972:18ff) observed that the quantifier in a nominal measure phrase has to be weak. We cannot say *most feet taller, most feet of yarn, ran most miles or most inches above the painting*. This restriction follows from (6) and the general prohibition on strong quantifiers in predicative noun phrases.

Adger(1994) notes that the ban on strong quantifiers extends to arguments of measure verbs (*weighs most ounces*). Adger discusses a number of other properties of the objects of measure verbs which lend further support to the idea that they are predicative. These include Rizzi(1990)’s observation that measure phrase arguments are sensitive to weak islands (*What don’t you think he saw?* versus *What don’t you think he weighs?*); the failure of measure phrases to passivize (*2 ounces was weighed by it*); Smith(1992)’s observation that measure phrases don’t show past participle agreement in French (*Les vingt grammes que cette lettre a pesé* (*es*) ‘the twenty grams that this letter has weighed’) and finally Adger’s own observation that in languages like Turkish, measure phrase arguments do not undergo specificity-sensitive scrambling.

If measure phrases are predicates of scalar intervals and noun phrases are not in general predicates of, or quantifiers over, scalar intervals, then we will need some help to put them together in the interpretation of a partitive or compound. Roughly following Parsons(1970) and Higginbotham(1994), we will make use of functions which map entities to intervals of a scale. The intention is to understand *three ounces of gold disappeared* along the lines of (7) below5:

\[ \text{Parsons analysis for } \textit{most gold is unmined} \text{ in addition makes use of maximization. Extending that idea to the present case, (7) should be replaced with (i) below, where I’ve used a totalizing operator, } \Sigma, \text{ (=Higginbotham(1994)’s} \]

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Here \( wt \) is a function that applies to objects with weight and returns an interval that begins at the bottom of the scale and whose length depends on the weight of the object in question. Different partitives will require different functions from entities to intervals. The interpretation of 2 hours of work requires, for example, a function assigning intervals on a scale of durations. The choice of function will be constrained by the meanings of the measure phrase and the noun phrase but it won’t always be determined by them. The interpretation of 2 ft of snow normally relies on a depth function, however, if, by chance, we are discussing a line of snow that someone has laid to create a boundary, then we make use of a length function to interpret He has already laid down 2 ft of snow.

I should briefly note here that, like Nerbonne(1995) and Krifka(1989), I imagine the analysis of measure phrases to extend to numerals. The interpretation of 9 boys makes use of a function from pluralities to intervals on a cardinality scale and 9 is a predicate of such intervals. Expressions like 9 more bottles, 9 too many point to the inclusion of numerals in the class of measure phrases (and similar observations lead to the idea that numeral-classifier combinations are measure phrases, see Kikuchi 2001 for relevant data). Likewise, many more boys suggests that many be treated like much with the added requirement that it apply exclusively to intervals of scales of cardinality or proportions.

At this point, we have proposals for the meanings of the parts of a partitive. The next task is to investigate how partitives are constructed. Before turning to that task, I want to briefly address a popular alternative to our semantics for measure phrases. Quine(1960:244-5) absurdly interrogates “Are miles alike? If so, how can they count as many? And if they cannot, what of the two hundred between Boston and New York?” He advises to replace “length of Manhattan = 11 miles” with a Carnapian “length-in-miles of Manhattan = 11”. This maneuver is applied to partitives by Krifka(1989), Higginbotham(1994) and Chierchia(1998:74) where sentences such as 6 oz. of salt melted are analyzed along the lines of:

\[
\exists y[ \text{salt}(y) \& \text{melted}(y) \& \text{oz}(y) = 6. ]
\]

This added sophistication is not relevant to anything that I have said or will say here. Maximization is acutely necessary, when considering paucal measure phrases (few, little, a bit).
Nobody, as far as I know, has explained how this view is supposed to connect with the semantics of expressions like 6 oz. heavier or 6 oz over the limit. Adjectival measure phrases present another problem for they do not correspond to a particular scheme of measurement and they do not take numeral arguments. Even nominal measure terms can get by without numeral arguments as in several ounces of salt. One could try to analyze these examples in terms of quantification over numbers. several might, for example, existentially quantify over numbers of a certain size. But that idea conflicts with what one finds when these quantifiers are inserted into contexts that clearly call for numerical arguments:

(9)  *Four plus several is less than 10.
    “there is a number greater than 2: 4 plus that number is less than 10.”
(10) *My three-year-old can count up to several.
(11) *There were exactly several groundhogs.
    ≠ “for some n greater than 2: there were exactly n groundhogs”

Finally, it is hard to explain the choice of plural ounces in the expression ten ounces of salt on the assumption that ten is a number-denoting argument of ounces (compare: ten is greater than six). On the theory proposed here, the extension of ounces includes pluralities, each of which consists of at least two intervals in the extension of ounce. 9 ounces is interpreted with a cardinality function, just like 9 boys.


Giusti(1997) posits two distinct positions where quantifiers such as Italian tutti ‘all’ and molti ‘many’ may be generated. The positions differ in terms of their order relative to determiners. These are depicted in the trees below:

(12) QP
    Spec
    Q’
    Q
    DP
    tutti
    i ragazzi
    all
    the books

*Lønning(1987:41) raises a related problem when he compares less than two kilos of cheese disappeared with the cheese that disappeared weighed less than two kilos. His proposal involves separating out two functions, one from objects to their weights and another that maps from weights to numbers. The first function is similar to our wt in (7).
Giusti observes that the two quantifier positions differ with respect to whether they permit the extraction of a pronoun:

(14)  ho visto molti ragazzi.
     I.have seen many boys

(15)  ne_i ho visti molti t_i
     of.them I.have seen many

(16)  ho visto i molti ragazzi.

(17)  *ne_i ho visti i molti t_i

With the analyses in (12)-(13), we explain this difference simply by taking *ne to be a DP.

In the tree in (13), Giusti follows the general program of Cinque(1994) in which adjectives are inserted in the specifier of a nominal functional projection. In those positions they agree with the noun through Specifier-Head agreement. Both simpatici and molti are masculine plural indicating that all functional heads bear the number and gender features of the projection. Now in (12), tutti similarly agrees with the head noun. Giusti(1997) argues that quantifiers are not functional, which means that in (12) we have an odd case of a lexical head agreeing with its complement. Moreover, as Delsing(1993) points out, this kind of approach means that categories selecting noun phrases would have to specify QP or DP or both. This suggests to me that we replace (12) with a structure in which Q is a functional head with tutti in its Specifier^7.

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With (18), we can now accommodate further cases. *too much of the rice* is generated with the phrasal *too much* in Spec, QP and the DP *the rice* in the complement of Q. Assuming that possessives are generated in Spec, DP (see Giusti 1997 and references therein), Jackendoff (1977:124)’s pair below follows immediately:

(19) *John’s many of those objections.
(20) John’s many objections.

*many* must be in Spec, AgrP in these examples, since it follows the possessive and hence is within a DP. This means we have a structure like in (13). In that case, there is no room for a DP to follow *many*, hence the ungrammaticality of (19).

Turning to nominal measure phrases, simplicity demands that we take them to fill these very same specifier positions. They too appear before and after determiners:

\[
\begin{array}{ll}
\text{i.} & \left[ \text{QP} \right. \left[ Q' \left[ \text{Q} \right. \left[ \text{DP} \right. \text{ha-sefarim} \right] \text{]} \right] \quad \text{ii.} & \left[ \text{QP} \right. \left[ \text{ha-sefarim} \right. \left[ Q' \left[ \text{Q} \right. \text{kul-am t} \right] \text{]} \right] \\
\text{all} & \text{the-book.Masc.P} & \text{the-book.Masc.Pl} & \text{all.3rd.Masc.Pl}
\end{array}
\]

Shlonsky’s idea is that in going from (i) to (ii), the DP *hasfarim* moves from the complement of Q to Spec, QP thereby triggering Spec-Head agreement showing up on *kol~kul*. But the number and gender marking on *kol~kul* bears no resemblance to agreement on nouns or adjectives (cf. *zol* ‘cheap’ / *zolim* ‘cheap-Masc-Pl, bul ‘stamp’ / *bulim* ‘stamps-Masc-Pl’) but is identical to the pronominal suffixes often found on nouns and prepositions (*axot* ‘sister’/*axotam* ‘their (Masc) sister’; *beyn* ‘between’/*beynam* ‘between them-Masc’). Assuming one goes from (i) to (ii) via DP movement, the affix on *kol* appears to be a resumptive pronoun, a device often used in Hebrew.
(21) What will I do with 2-lbs of the cottage cheese?
(22) What will I do with the 2-lbs of cottage cheese?

Recall that *ne* cliticization was taken to be diagnostic for the presence of a DP inside a QP. Assuming that nominal measure phrases occupy Spec,QP leads to the correct prediction that they too licence this type of cliticization. Proudfoot and Cardo teach that when the shopkeeper asks if you want some of the bread, you can reply:

(23) si, *ne*$_i$ vorrei [QP [un chilo] [Q' [DP t$_i$]]]
    yes, CL-gen I-would-like a kilo

By way of summary, let us distill out the crucial claims. There are at least three functional levels in the projection of a nominal: Q(antity), Agr(eement) and D(eterminer). Quantifiers or measure phrases can at least be Specifiers of QP and AgrP. Following the logic of Grimshaw(1991,2000), we further stipulate that AgrP may not dominate DP or QP and that DP may not dominate QP. This is perhaps all that needs to be said. Giusti further stipulates selectional requirements for various quantifiers, but this may not be necessary. This setup allows that quantifiers in QP may combine with DPs, but they may also combine with AgrPs or NPs. In section 3, we deduced from monotonicity requirements that measure phrases in partitives could combine either with NPs or with definite DPs when a partitive-*of* is present. A full treatment of *all* is beyond the bounds of this paper. However, assuming Brisson(1998)'s semantics, we capture the contrast between *all the boys* and *the all boys* (for more discussion along these lines, including expressions such as *all men*, see Matthewson(2001), Zamparelli(1996)).

We close this section with some speculations on *of*. Suppose that *of* may be inserted in the head of a functional projection. In *2 ounces of salt*, it shows up in the head of QP, while in *the 2 ounces of salt*, it fills the head of AgrP. In the first case, the measure phrase *2 ounces* is the Specifier of QP. As such, it is meant to agree with the head Q. But the measure phrase itself is headed by a noun. Assuming that agreement is an asymmetric relation – one party is agreeable and the other demands agreement – then we have a problem. The measure phrase is being asked to agree, when it is a trigger for agreement. In this case then, *of* is a disagreement marker which steps in to solve this problem$^8$. This is only necessary when the head of the measure phrase is nominal. No problem arises when it’s an adjective (Gawron 2002). This hypothesis covers not only things like

$^8$ Sanchez(1996) posits the following constituent structure for the Spanish *ladrona de joyas* ‘jewelry thief’

i. D$_0^P$ [PredP [NP ladrona$_j$]] Pred$_0^P$ + Agr$_i^P$ de [AgrP [NP joyas] e$_i$ [NP$_j$]]

She comments “the element in Spec of AgrP is another NP. As the NP in this specifier position is strongly marked for agreement features in Spanish a dummy preposition *de* ‘of’ is used to avoid a clash in features.”
2 ounces of versus too much *of, but it also covers idiomatic measure phrases that use an indefinite article:

MP w/adj head       a little (*of) soap       a few (*of) men
MP w/noun head      a bit *(of) soap        a number *(of) men

If the pseudopartitive *of adjudicates between competing agreement triggers, one might wonder what happens in languages without a pseudopartitive *of. One alternative is to simply omit number marking on the measure term, as in the following German example:

(24) zwei Pfund/*Pfunde Salz [from Vos(1999:52)]
    two   pound/pounds   salt
    ‘two pounds of salt’

The preceding account could be extended to true partitive *of but it needn’t be. Jane Grimshaw(pc) suggested taking PP to form a layer of the extended nominal projection below QP but above DP (see Grimshaw 1991,2000 for arguments that PPs are extended nominal projections). Under this view, true partitive QPs might be formed with true prepositions:

(25) \[
    \text{[QP } \text{many } [Q^* [Q^e] [PP } [of] \text{ [DP the trees]]]}
\]

Since measure phrases in partitives are always monotonic, we now have the first part of our generalization. In a nominal projection, the area above NP is exclusively zoned for measure phrases that are monotonic.

Next we turn to the syntax of measure phrase compounds. Recall that I concluded from the absence of *of and of number marking in expressions like 7 pound baby that these were compounds. These expressions are usually thought to be complex words, formed pre-syntactically. But Liberman and Sproat(1992) argue that such a conclusion is unwarranted. The lack of number marking and other functional morphology on a nominal modifier may simply be the result of its presence inside of NP (see position of simpatici in (13)). On their view, stress facts are a more faithful indicator of word-like status. While the final stress in defective nóvel follows from phrasal stress rules, the initial stress in détective novel follows from a rule of stress that works like other word-level stress rules. Liberman and Sproat conclude that detective novel is a member of the same category as the word novel, what they call N°. By this criterion, some Noun-Noun collocations are N°s and some are phrases. tóaster oven, with initial stress is an N°, but brick óven, with final stress, is a phrase and so is 7 pound báby. In effect, 7 pound is combined syntactically with baby in the same way that chubby is in chubby baby.

---

9 Lack of functional morphology includes the preference for one inch cubes over *an inch cubes.
This view coheres with what one finds for the distribution of non-monotonic measure phrases in languages close to English. Although noun-noun compounds are possible in Spanish (hombres rana ‘frog men’ perro policía ‘police dog’ países satélite ‘satellite countries’) they are not where you find non-monotonic uses of measure phrases. Instead what you find is verbally similar to the partitive but with the order reversed:

<table>
<thead>
<tr>
<th>Monotonic</th>
<th>Non-Monotonic</th>
</tr>
</thead>
<tbody>
<tr>
<td>dos centímetros de cable</td>
<td>agua de dos grados</td>
</tr>
<tr>
<td>2 cm. de cable</td>
<td>water 2 degrees</td>
</tr>
<tr>
<td>‘2 centimeters of cable’</td>
<td>‘2° water’</td>
</tr>
<tr>
<td>*dos grados de agua</td>
<td>*agua de dos litros</td>
</tr>
<tr>
<td>* 2 degrees of water</td>
<td>water 2 liters</td>
</tr>
</tbody>
</table>

This alternative to compounds occurs outside Romance as well:

<table>
<thead>
<tr>
<th>Monotonic</th>
<th>Non-Monotonic</th>
</tr>
</thead>
<tbody>
<tr>
<td>een centimeter staaldraad</td>
<td>staaldraad van een centimeter</td>
</tr>
<tr>
<td>one cm. wire’</td>
<td>wire van one cm.</td>
</tr>
<tr>
<td>‘1 cm. of wire’ (length)</td>
<td>‘1 cm. wire’ (diameter)</td>
</tr>
</tbody>
</table>

And it is probably what you have in the English a group of three men meaning ‘a three man group’. German and Russian provide morphological evidence for the view that non-monotonic measure phrases are treated like pre-nominal adjectives. They are formed with an adjectival suffix:

<table>
<thead>
<tr>
<th>Monotonic</th>
<th>Non-Monotonic</th>
</tr>
</thead>
<tbody>
<tr>
<td>foif liter wasser</td>
<td>foigredigs wasser</td>
</tr>
<tr>
<td>5 liters water</td>
<td>5 degree Adj water</td>
</tr>
<tr>
<td>‘5° water’</td>
<td>‘foifliterigs wasser’</td>
</tr>
<tr>
<td>*foif graad wasser</td>
<td>*5 liter Adj water</td>
</tr>
<tr>
<td>*5 degree water</td>
<td></td>
</tr>
<tr>
<td>desiat’ santimetrov vody</td>
<td>desiatigradusnaja voda</td>
</tr>
<tr>
<td>10 cm. pl water-gen</td>
<td>10-degree-Adj water</td>
</tr>
<tr>
<td>‘10 cm water’</td>
<td>‘10° water’</td>
</tr>
<tr>
<td>*desiat’ gradusov vody</td>
<td>*desiatigradusnaja voda</td>
</tr>
<tr>
<td>*10° of water</td>
<td>10-cm-Adj water</td>
</tr>
<tr>
<td></td>
<td>‘*10 cm water’</td>
</tr>
</tbody>
</table>

My conclusion then is that measure phrases, when used non-monotonically, are combined in the syntax, but at a lower position than when they
are used monotonically. Referring to the tree in (13), a non-monotonic measure phrase occurs inside NP, like the adjective *simpatici*. This contrasts with a monotonic measure phrase which occurs outside of NP, in the functional portion of the projection.\(^{10}\)

6. Two kinds of adjectives.

In the introduction, it was observed that *too much gold* can’t mean gold which is too dark. This shows that although *much* is free to chose among various scales, it cannot be used as a non-monotonic modifier. This restriction also entails that while you can have *too much pork (by weight)* you can’t say *too much pig* to mean a pig that is too heavy. A singular count noun *pig* allows only for a non-monotonic interpretation and, as we have just said, *much* is forbidden to participate in such an arrangement. *much* is exclusively monotonic and, because of the way cardinality works, so is *many*. But while these adjectives\(^{11}\) are used inside nominal projections exclusively as monotonic modifiers, most other adjectives are used exclusively as non-monotonic modifiers. This is easy to see in the case of adjectives like *red* or *cold*. The properties that are relevant to their application do not track part-whole relations. This has already been observed in connection with temperature and color works similarly. What is not so obvious is that the restriction to non-monotonicity applies as well to adjectives like *heavy*, *deep* and *extensive*, all of which are tied to properties that do track part-whole relations. Given that these adjectives track part-whole relations, in order to be used non-monotonically, the kind of substance-noun they combine needs to be carefully chosen. To see how this is going to work, let us review what happens when measure phrases that track monotonic properties are *syntactically* constrained to produce non-monotonic interpretations. *20 oz water* is out because weight is monotonic with respect to water-parts. *20 oz ice-cube* works because count nouns come with no part structure and so they insure the absence of monotonicity. *20 oz ice-cubes* is possible, but only on a distributive reading, where it is a plural of *20 oz ice-cube*. The adjectives that are associated with part-whole related properties are similarly restricted to combining with singular count nouns or with plurals with a distributive interpretation. So if I melt a heavy, carcinogenic ice-cube, I’m likely to get carcinogenic water, but I won’t get *heavy water*. When an adjective combines with a plural noun it can in principle have a distributive or a collective reading. If Jack told inconsistent stories, it could either be because the stories conflicted with one another (collective), or because each story contained an inner contradiction (distributive). But this ambiguity is lost in the phrase *heavy ice-cubes* which must be understood distributively (it can’t be the combined weight of the ice-cubes that is excessive). From the felicity of 2

\(^{10}\) I’m using terms like ‘monotonic measure phrase’ to mean one that is used as a modifier, whose application is based on a property which is monotonic relative to the part-whole relation determined by the noun

\(^{11}\) In English, the motivation for calling *much* and *many* adjectives is that they combine with *very* and they head degree constructions: *so many, too much, that much*. Cross linguistically adjectives with similar meaning and grammar show adjectival number and gender marking.
inches of snow, we determined that talk of falling snow implies a part-whole structure in terms of layers. That explains the oddness of saying that deep snow fell on Rhode Island last night. The closest we can come to that is to say that a deep layer of snow fell, where we use a singular count noun. And while George may have produced an extensive report on this issue, he could not have done so after having read extensive literature. And if he had extensive discussions, then each of them had to be extensive.

Sound and light are interesting in this regard. alot of light and alot of noise are pseudopartitives apparently based on intensity, indicating that intensity is monotonic for light and noise. Correspondingly, we find the following pattern of adjectival judgements: The box was emitting light contrasts with #The box was emitting dim light and He was making noise contrasts with *He was making loud noise. The distributively interpreted plural alternative is the closest one can come: He was making loud noises.

Compare now the expressions cheap wine and cold wine. One way to describe the contrast is that cheap refers to the kind, while cold refers to the stuff itself. But there is another explanation. Temperature is non-monotonic, hence it works fine as the basis for an adjective applying to wine. Price, on the other hand, tends to be monotonic. The more you drink, the more you pay! So cheap wine can’t be used to describe a portion of wine whose amount was small enough so as to fall well within your budget. But there is another sense of price, one in which you think in terms of cost per unit. This sense of price is monotonic and it’s the one you get in the possible interpretation of cheap wine.

On the basis of these kinds of judgments, I conclude that adjective modifiers divide into two classes, a closed class of adjectives including much which are exclusively monotonic, and a large, open class of adjectives which are exclusively non-monotonic. Before discussing the ramifications of this division, I want to address a question that may be plaguing some readers. All of the so-called non-monotonic adjectives discussed above can be used predicatively and in that case they appear to freely combine with mass expressions or collectively understood plurals:

(28) The water was heavy.
(29) The bottles were heavy. (collective reading)
(30) The literature is extensive.

Recall that whether or not a modification counts as monotonic, depends upon the part-structure of the argument of the modifier. This was the motivation for claiming that nouns denote structured sets. Standard views take the subjects of (28)-(30) to either be entity denoting or quantifiers over entities. This means that the meanings of the predicates in these examples are applying not to structured sets but to single entities. So, as in the case of singular count noun arguments,
these all count as non-monotonic applications of these adjectives, since there is no part-whole structure to be monotonic on.\textsuperscript{12}

Having divided our adjectives into two classes, we now might wonder where the division comes from. I’d like to show that it doesn’t follow from the concepts underlying them, but is an added feature that relates to the lexical/functional distinction that is pervasive in grammar. In (31), I’ve given a meaning for \textit{much} as used in \textit{too much gold (by weight)} where it occurs inside a noun phrase with a weight based measure function. MUCH stands for a predicate of scalar parts (see section 4):

\begin{equation}
\lambda X \lambda z[ X(z) \& \text{MUCH}(\text{wt}(z)) ]
\end{equation}

(31) follows the line of reasoning expanded on in section 4, but it is incomplete. To see this, notice that (31) is essentially the meaning of \textit{heavy} and (\textit{light} would look the same with MUCH replaced by LITTLE). In effect, (31) captures what \textit{much} (in a weight context) has in common with \textit{heavy} and it misses the differences between the two. What we need is another piece of meaning having to do with monotonicity:

\begin{align}
\text{\textit{much}} : \lambda X \lambda z[ X(z) \& \text{MUCH}(\text{wt}(z)) \& \text{\textit{wt} is monotonic on X} ] \\
\text{\textit{heavy}} : \lambda X \lambda z[ X(z) \& \text{MUCH}(\text{wt}(z)) \& \text{\textit{wt} is non-monotonic on X} ]
\end{align}

Where does this other piece of meaning come from? I claim it is related to the elusive lexical-functional distinction. This distinction crops us at every level of grammar: it plays a role in the ordering of morphemes in a word, it has been implicated in the construction of phrases (as already alluded to in section 5), and it is a determining factor in the assignment of stress and accent, to name just a few examples. In addition, there is psycho- and neuro-linguistic evidence for the psychological reality of this distinction. There is a strong intuition that the distinction has a semantic basis, but it is not always easy to pin that down. In this case, however we have a precise characterization. Functional adjectives like \textit{much} are monotonic, while lexical adjectives are non-monotonic. The fact that there are so few monotonic adjectives is yet another hallmark of their functionality.

7. Putting it all together

In section 5, we adopted a view of nominal phrases by which they divide into a lower, lexical portion and a higher, functional portion. We said that measure phrases with a monotonic interpretation went in the functional portion and those

\textsuperscript{12} Ron Artstein(pc) suspects that in \textit{the heavy bottles} the adjective \textit{heavy} could have a collective reading if it is interpreted as a non-restrictive modifier. If so, then we would have to analyze such modifications as cases in which the adjective’s meaning does not apply directly to the meaning of the noun.
with a non-monotonic interpretation went inside the lexical portion, labeled NP in (13).

In section 6, we appealed again to the lexical/functional distinction, this time to effect a division within the class of adjectives. And again, lexical paired with non-monotonic and functional with monotonic.

In order to bring these two ideas together, we need to say more about what happens with nominal measure phrases like *one inch*. In section 4, we argued that these measure phrases are predicates of scalar intervals. In order to combine them with a substantive, they must be augmented with a measure function from stuff to scales. This augmentation is the semantic result of converting them into modifiers. And here there is a choice, they can either become functional modifiers, by the rule in (34), or lexical modifiers, by the rule in (35). \( \mu \) is a variable over measure functions:

\begin{align*}
\text{(34)} & \quad \text{NMP} \rightarrow \text{Functional Modifier} \\
& \quad \text{mp} \rightarrow \lambda X \lambda z [X(z) \& \text{mp}(\mu(z)) \& \mu \text{ is monotonic on } X.]
\end{align*}

\begin{align*}
\text{(35)} & \quad \text{NMP} \rightarrow \text{Lexical Modifier} \\
& \quad \text{mp} \rightarrow \lambda X \lambda z [X(z) \& \text{mp}(\mu(z)) \& \mu \text{ is non-monotonic on } X.]
\end{align*}

As (26) shows these rules may have a morphological reflex. The German derivational (= lexical) affix *igs* is added to the noun phrase when (35) applies.

Finally, we can take it as a matter of syntax, that functional modifiers must appear in the functional portion of the nominal projection, and lexical modifiers go in the lexical portion.

8. Conclusion

Loudness, pungency, intensity, temperature, weight and volume all name properties that can be had in varying degrees. These properties can be divided into two classes. There are some, like weight, whose degree is a reflection of amount. And there are others like temperature whose degree is not a good gauge of amount. We called the former monotonic, because their degree is monotonic on the part-whole relation. The latter are called non-monotonic. This distinction is linguistically relevant.

Mass nouns and plural nouns denote structured sets. The structure is given by a part-whole relation. Depending on the linguistic context, the relation may be as general as material-part or as specific as sublayer-of-snow. Count nouns denote unstructured, ‘atomic’ sets. This matters for monotonicity. In looking at the interpretation for an extended noun phrase, the particular relation encoded in the noun will be the one relative to which a property will be said to be monotonic or non-monotonic.
Modifiers of nouns can be either functional or lexical. The functional ones occur in specifier positions in the upper, functional portions of the extended projection, while the lexical ones occur as specifiers in the lower, lexical portion. The lexical modifiers form an open class including red, cold and heavy, while the functional ones are derived from a closed class including much and many. Functional modifiers must be used to produce interpretations based on a property that is monotonic relative to the part-whole relation given by the head noun. Lexical modifiers must be used to produce interpretations based on a property that is non-monotonic relative to the part-whole relation given by the head noun.

Measure phrases occur in various syntactic contexts, most commonly in comparatives and in noun phrases. They denote predicates of scalar intervals. two ounces applies to intervals that are twice the size of those that one ounce applies to. When a measure phrase is used to modify a noun phrase, it is augmented with a function whose range is scalar intervals. This augmentation is the semantic half of each of two rules that produce modifiers of nouns out of scalar predicates. One of these rules produces a functional modifier and the other produces a lexical modifier.

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